

Formation of He²⁺ shell-like distributions downstream of the Earth's bow shock

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[1] When the incident solar wind He²⁺ and H⁺ distributions cross the electrostatic potential at the shock, they are decelerated differentially due to their different charge- to-mass ratios. This differential slowing will produce a He²⁺ ring-beam distribution immediately downstream from a quasi-perpendicular shock. In this letter, we perform one-dimensional (1D) hybrid simulations and investigate the evolution of the He²⁺ ring-beam distribution in magnetized plasma. The plasma is composed of three components: H⁺, He²⁺ and electrons, where H⁺ has a velocity distribution with large perpendicular temperature anisotropy. It is shown that both the He²⁺ ring-beam distribution and H⁺ distribution with large perpendicular temperature anisotropy can excite ion cyclotron waves with propagation direction parallel to the ambient magnetic field, and then the waves pitch-angle scatter the He²⁺ ions. However, only the ion cyclotron waves excited by the He²⁺ ring-beam distribution can transform He²⁺ into shell-like distribution. The results can explain the He²⁺ shell-like distributions downstream of the Earth's bow shock, which have already been observed with the AMPTE/CCE and ISEE spacecraft. **Citation:** Lu, Q. M., and S. Wang (2005), Formation of He²⁺ shell-like distributions downstream of the Earth's bow shock, *Geophys. Res. Lett.*, 32, L03111, doi:10.1029/2004GL021508.

1. Introduction

[2] The bow shock is formed upstream from the Earth in order to slow the incoming solar wind plasma from supersonic to subsonic and to deflect this plasma around the magnetospheric obstacle. Although the structures of this collisionless shock and the evolution of the solar wind proton distributions across the bow shock have been extensively studied in recent years by analyzers on orbiting spacecraft and by theoretical investigations [Burgess, 1989b; Schwartz *et al.*, 1992; Matsukiyo and Scholer, 2003; Lembege *et al.*, 2004], the behavior of the solar wind minor ions was studied only by a few papers [Shelley *et al.*, 1976; Peterson *et al.*, 1979; Ogilvie *et al.*, 1982; Winske *et al.*, 1985; Burgess, 1989a; Motschmann *et al.*, 1991; Motschmann and Glassmeier, 1993; Fuselier *et al.*, 1988, 1991; McKean *et al.*, 1996; Fuselier and Schmidt, 1997].

[3] These minor ions in the solar wind usually have very low concentrations relative to H⁺. Among these minor ion species, He²⁺ is the most common solar wind ion after H⁺, which constitutes typically about 4% of the total solar wind ion density in number. Bow shock theory and simulations

have shown that these minor ions don't adversely affect the shock structures and can be treated approximately as test particles at the shock. Fuselier and Schmidt [1997] proposed a simple He²⁺ injection model, in which the bow shock is considered as an infinitely thin electrostatic potential at the shock. They ignore any effects that might arise because the velocities of the distributions change over a finite shock thickness. The electrostatic potential at the shock causes H⁺ slow more than He²⁺ because H⁺ has larger charge-to-mass ratio, and thus in the downstream region there is a different velocity between H⁺ and He²⁺ if they are assumed to have the same bulk velocity in the solar wind. He²⁺ is "injected" with its velocity relative to H⁺ into the immediate downstream region, which produces a He²⁺ ring-beam distribution immediately downstream from a quasi-perpendicular shock.

[4] The observations of He²⁺ and other minor ions in the downstream of the shock have shown that they have shell-like distributions. Peterson *et al.* [1979] found that the He²⁺ distribution have a flat top at low velocities in the downstream of the shock, which can be interpreted as an unresolved or filled He²⁺ shell. Fuselier *et al.* [1988, 1997] reported He²⁺ and O⁶⁺ shell-like distributions downstream from the bow shock and a larger radius of O⁶⁺ shell than that of He²⁺. Hybrid simulations also show that He²⁺ has shell-like distributions in the downstream of quasi-perpendicular and quasi-parallel shocks [Motschmann and Glassmeier, 1993; Trattner and Scholer, 1993]. In this paper, with a 1D hybrid simulation code, we investigate the evolution of the He²⁺ ring-beam distribution in the downstream of quasi-perpendicular shocks.

2. Simulation Model

[5] A one-dimensional (1D) hybrid code [Winske *et al.*, 1985] is employed in our simulations. The plasma consists of two ion components (H⁺ and He²⁺) and the electron component. He²⁺ contains 4% of total ion number density. Initially, the electron fluid bears zero average flow speed, and H⁺ satisfies bi-Maxwellian velocity distribution with $T_{\perp p}/T_{\parallel p} > 1$ (the subscripts \parallel and \perp denote the directions parallel and perpendicular to the ambient magnetic field). He²⁺ is assumed to satisfy ring-beam distribution and its initial temperature is four times of the parallel temperature of H⁺, which is consistent with the observations in the solar wind [Feldman *et al.*, 1996; Gary *et al.*, 2001]. According to the He²⁺ injection model of Fuselier and Schmidt [1997], the shock can be modeled as an effective potential. Due to their different charge to mass ratios, the shock slows H⁺ more than He²⁺, which results in a relative velocity between H⁺ and He²⁺ just downstream of the collisionless shock. The

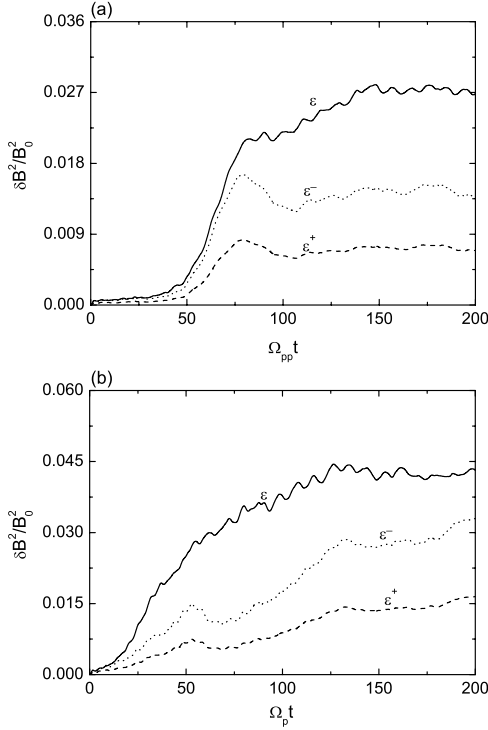


Figure 1. The time history of $\varepsilon = \delta B^2/B_0^2$ ($\delta B^2 = B_y^2 + B_z^2$), the total magnetic field energy, ε^+ , the magnetic field energy of positive helicity, ε^- , the magnetic field energy of negative helicity. (a) $T_{\perp p}/T_{\parallel p} = 1.5$, (b) $T_{\perp p}/T_{\parallel p} = 2.7$.

difference of their velocities is called the injection velocity. By considering a special case, we can obtain an estimation of the magnitude of the injection velocity. For a supercritical, high Mach number, nearly perpendicular shock, the injection speed is about $0.4|\mathbf{V}_{sw}|$ ($|\mathbf{V}_{sw}|$ is the amplitude of the solar wind speed) [Fuselier and Schmidt, 1997]. In our simulation we choose the He²⁺ injection speed as $2.2V_A$ (V_A is the local Alfvén speed) and the injection angle (the angle between the injection speed and downstream magnetic field) $\alpha = 80^\circ$.

[6] The simulations are performed in the center-of-mass frame, and periodic boundary conditions are used. The background magnetic field is assumed to be $\mathbf{B}_0 = B_0\hat{x}$. We use 128 grid cells with 800 particles per cell for each ion component. The grid size is $\Delta x = 1.0c/\omega_{pp}$, where c/ω_{pp} is the ion inertial length. The time step is taken to be $\Omega_p t = 0.04$, where Ω_p is the proton gyro frequency. The proton plasma $\beta_p = 0.5$, where β_p is the ratio of kinetic pressure of the protons to magnetic pressure.

3. Simulation Results

[7] Both the He²⁺ ring-beam distribution and H⁺ distribution with large perpendicular temperature anisotropy can excite electromagnetic waves. According to the method developed by Terasawa *et al.* [1986], we can separate the wave fluctuations into positive and negative helical parts. For positive helicity, forward propagating waves will be right-hand polarized (magnetosonic waves), whereas waves propagating backward will be left-hand polarized (Alfvén/ion cyclotron waves). Similarly, forward propagating waves

with negative helicity will be left-hand polarized (Alfvén/ion cyclotron waves), whereas the backward propagating ones will be right-hand polarized (magnetosonic waves) [Araneda *et al.*, 2002]. In our simulations, we choose two different values for the H⁺ temperature anisotropy: (a) $T_{\perp p}/T_{\parallel p} = 1.5$, (b) $T_{\perp p}/T_{\parallel p} = 2.7$. In case (a), the dominated waves are excited by the He²⁺ ring-beam distribution. In case (b), the dominated waves are excited by the large H⁺ perpendicular temperature anisotropy. Figure 1 shows the time history of $\varepsilon = \delta B^2/B_0^2$ ($\delta B^2 = B_y^2 + B_z^2$), the total fluctuating magnetic field energy, ε^+ , the fluctuating magnetic field energy of positive helicity, ε^- , the fluctuating magnetic field energy of negative helicity, for case (a) and (b). Both the positive and negative helical waves can be excited, and the negative helical waves have larger amplitudes than that of positive helical waves. For case (a), the waves begin to be excited at $\Omega_p t \sim 50$, and saturate at $\Omega_p t \sim 80$. For case (b), the waves begin to be excited at $\Omega_p t \sim 20$, and saturate at $\Omega_p t \sim 120$. At the quasi-equilibrium stage, the average amplitudes of waves are about $\delta B/B_0 \approx 0.16$ and 0.21 for case (a) and case (b) respectively.

[8] Detailed analysis shows that both the positive and negative helical waves are left-hand polarized. The positive helical waves propagate backward while the negative helical waves propagate forward. Therefore both the positive and negative helical waves are ion cyclotron waves. Actually the waves excited in case (a) are similar to the waves excited by He²⁺ bi-Maxwellian distributions with large perpendicular temperature anisotropy [Gary *et al.*, 1994]. In Figure 2 we

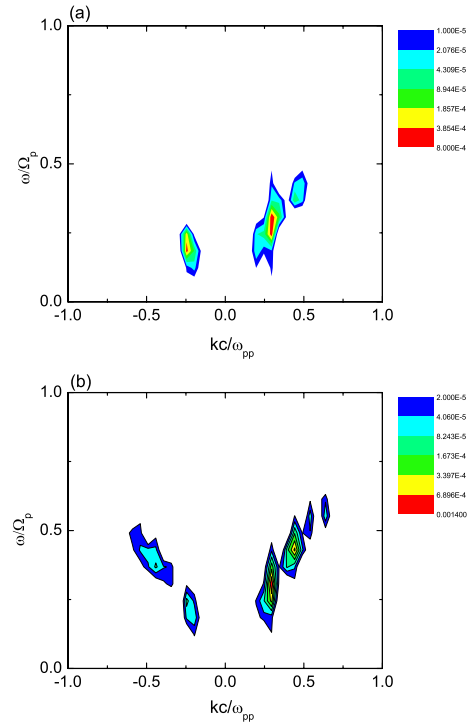


Figure 2. The characteristics of $\omega-k$ diagram obtained by Fourier transformation of the magnetic fields in the y direction from $\Omega_p t = 0$ to $\Omega_p t = 102.4$, the negative k means that the waves propagate backward whereas the waves with positive k propagate forward. (a) $T_{\perp p}/T_{\parallel p} = 1.5$, (b) $T_{\perp p}/T_{\parallel p} = 2.7$.

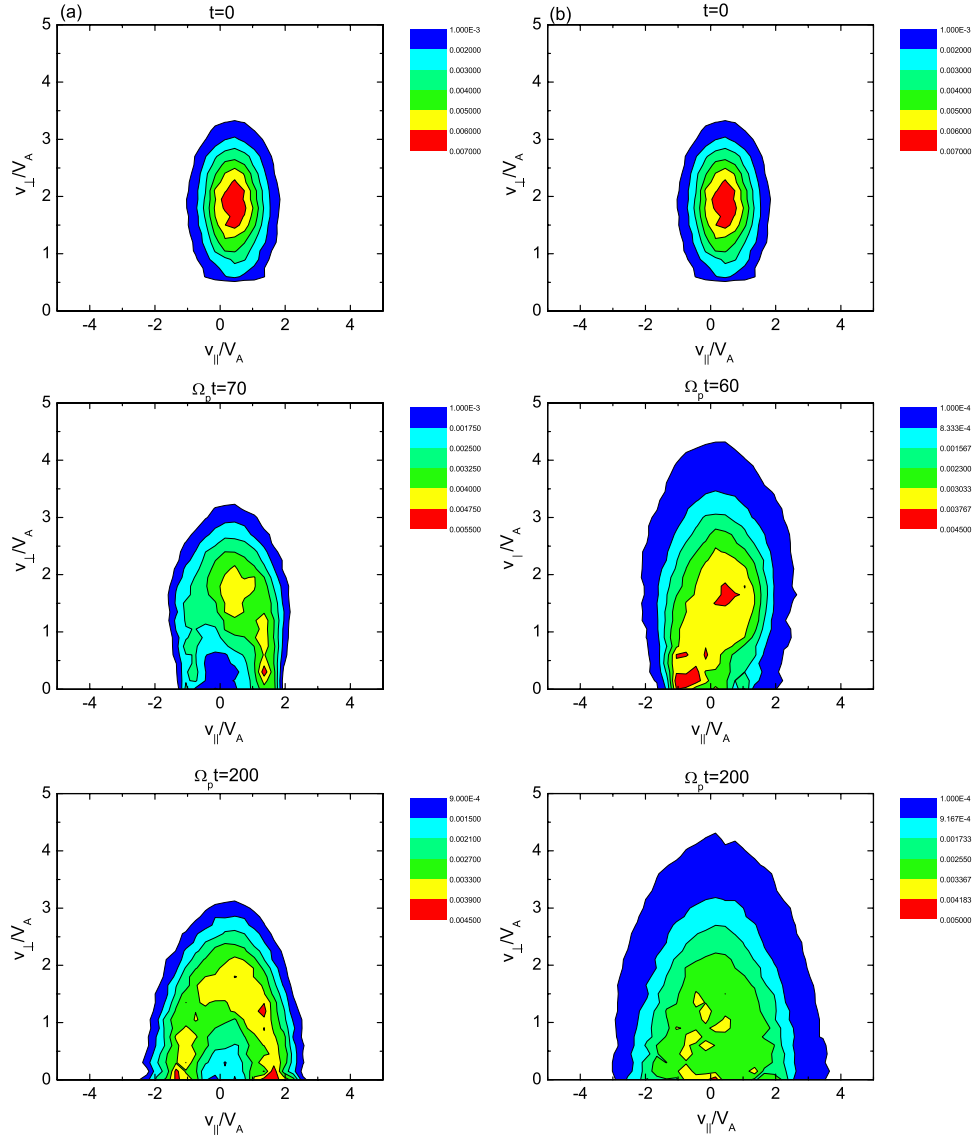


Figure 3. The He²⁺ velocity distributions at different times. In the figure, $v_{\parallel} = v_x$ and $v_{\perp} = \sqrt{v_y^2 + v_z^2}$. (a) $T_{\perp p}/T_{\parallel p} = 1.5$, (b) $T_{\perp p}/T_{\parallel p} = 2.7$.

show the characteristics of $\omega-k$ diagram obtained by Fourier transformation of the fluctuating magnetic fields B_y^+ and B_y^- from $\Omega_p t = 0.0$ to $\Omega_p t = 102.4$. In case (a), the frequencies of the waves excited by the He²⁺ ring-beam distributions is below the He²⁺ cyclotron frequency, while in case (b) the frequencies of the waves excited by the H⁺ large perpendicular temperature anisotropy can exceed the He²⁺ cyclotron frequency.

[9] The excited waves can pitch-angle scatter He²⁺ and transform its velocity distribution. Figure 3 describes the evolution of the He²⁺ velocity distribution $f(v_{\parallel}, v_{\perp})$ at different times for case (a) and (b). Initially, the He²⁺ ions concentrate near $v_{\parallel} = 0.38V_A$ and $v_{\perp} = 2.17V_A$, which is a ring-beam distribution with the radius $2.2V_A$. For case (a), with the excitation of the ion cyclotron waves, He²⁺ is pitch-angle scattered by the ion cyclotron waves. The radius of the ring-beam decreases, and at the same time the velocities in the direction parallel to the ambient magnetic field increases. At $\Omega_p t \sim 100$, a shell-like velocity distribution

of He²⁺ is formed with the radius about $1.5V_A$, which seems to last very long time. Even at the end stage of our simulations it still persists. However for case (b), at the quasi-equilibrium stage the He²⁺ distribution approximately satisfies a Maxwellian function, not a shell-like distribution.

4. Summary and Discussions

[10] Due to their different charge to mass ratios, the incident solar wind H⁺ and He²⁺ slow differentially across the boundary of the shock, which can form a He²⁺ ring-beam distribution in the downstream of the quasiperpendicular collisionless shock. In this letter, with a 1D hybrid simulation code we investigated the evolution of the He²⁺ ring-beam distributions in magnetized plasma where the H⁺ component has a large perpendicular temperature anisotropy. The results demonstrate that both the He²⁺ ring-beam distribution and H⁺ distribution with large perpendicular temperature anisotropy can excite the left-hand

polarized ion cyclotron waves propagating parallel and anti-parallel to the ambient magnetic field. However, it is the ion cyclotron waves excited by the He²⁺ ring-beam distribution that can pitch-angle scatter He²⁺ into shell-like velocity distribution with the radius a little smaller than that of its initial ring-beam distribution.

[11] Observations with AMPTE/CCE and ISEE spacecraft have shown that He²⁺ have shell-like velocity distributions downstream of the Earth's bow shock [Fuselier *et al.*, 1988; Fuselier and Schmidt, 1997], and computer simulations have also found the He²⁺ shell-like distributions in this area [Motschmann and Glassmeier, 1993]. It is generally accepted that the electromagnetic waves downstream of shock scatter the He²⁺ from ring-beam distributions to shell-like distributions. However, it is still unclear which kind of waves scatters He²⁺ into shell-like distribution. Our simulation results suggest that He²⁺ shell-like velocity distributions are formed by the waves excited by its own ring-beam distributions. In our study, we ignore the thickness of the shocks and perform the 1D hybrid simulation in the downstream frame which moves with the average speed of the protons. If the shock thickness is considered, the formation process of the He²⁺ shell-like distributions could be more complicated than what we have described. The ring-beam and shell-like distributions of He²⁺ may be occur simultaneous in the downstream of the shock and form a nongyrotropic ring distribution in the downstream frame as pointed by McKean *et al.* [1995b]. The waves and particle evolution downstream of quasi-perpendicular shocks have also been studied by McKean *et al.* [1995a, 1996] with a 2D hybrid simulation, and the shock is also included in their model. They found that the large H⁺ temperature anisotropy behind the shock overshoot can excite the proton cyclotron waves, which are then convected to downstream with the average speed of the protons. If it is correct, a 1-D simulation is not appropriate to describe the excitation and propagation of the proton cyclotron waves downstream of a shock. However, in their study the He²⁺ are heated in the direction perpendicular to the ambient magnetic field through absorption of proton cyclotron waves and become gyrotropic. The dynamics of He²⁺ is controlled by the proton cyclotron waves, which is similar to our case (b). When the evolution of the He²⁺ velocity distribution is dominated by the waves excited by the He²⁺ ring-beam distribution (like our case (a)), a 1-D simulation model as presented in this letter can describe the evolution of He²⁺ velocity distributions no matter how the proton cyclotron waves are excited.

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